

Data assimilation of gas measurements in TCAM model simulations over Northern Italy

C. Carnevale, G. Candiani, G. Finzi, E. Pisoni, M. Volta

Department of Information Engineering
University of Brescia

TFMM Meeting 13-14/05, Larnaca



1 Data Assimilation Overview

- General definition
- Optimal Interpolation

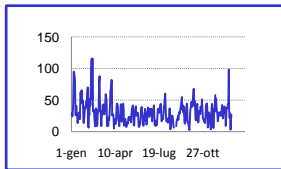
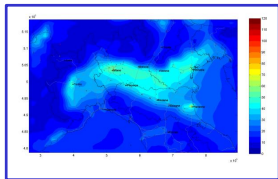
2 Test cases

- Off line DA
- On line DA

3 Conclusions

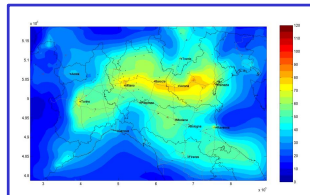
Data assimilation

INPUT



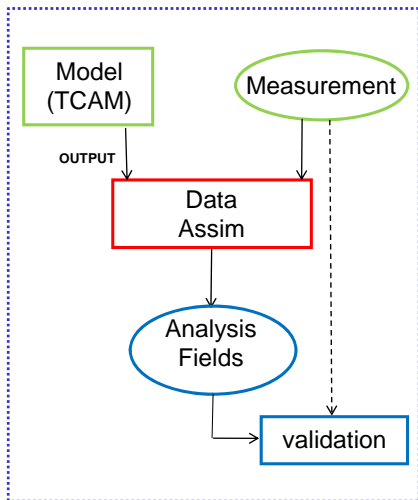
Data
Assimilation

OUTPUT

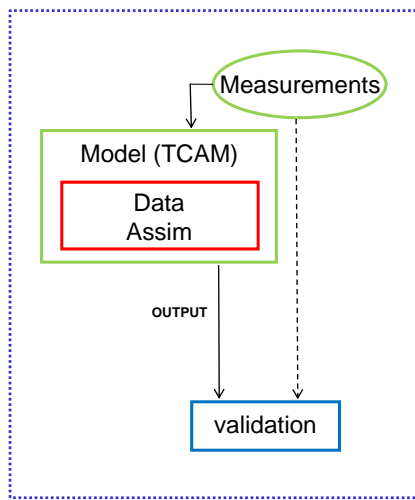


On line VS Off line

OFF-LINE



ON-LINE





- Residual Inverse Distance Weighting;
- Residual Co-Kriging;
- Optimal Interpolation;
- Ensemble Kalman Filter;
- 4D var.

Data Assimilation Techniques



- Residual Inverse Distance Weighting;
- Residual Co-Kriging;
- **Optimal Interpolation**;
- Ensemble Kalman Filter;
- 4D var.

Fundamental equations

$$x_a = x_b + K(y - Hx_b)$$

$$K = BH^T(HBH^T + R)^{-1}$$

x_a : analysed field

x_b : background field

y : measurements (ground/lidar/satellites)

H : output operator

K : OI gain

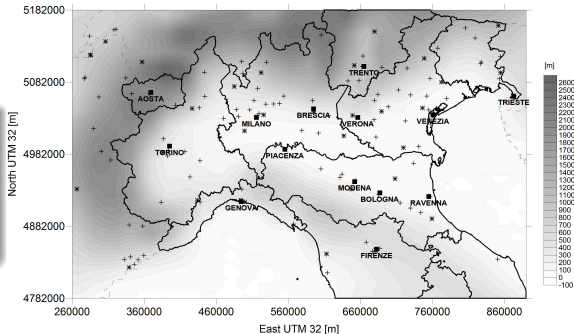
B : background error covariance matrix

R : measurement error covariance matrix

Test case setup

Domain Info

- Dimension: $640 \times 430 \text{ km}^2$;
- Horiz. Resolution: 10 km ;
- Ground station OI: +;
- Ground station validation: *;

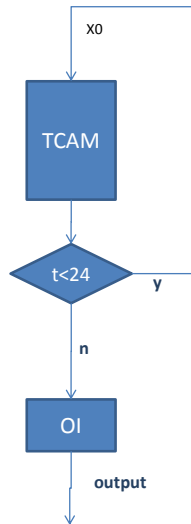


- 3D Eulerian Model;
- Horizontal Transport: Chapeau function + Forester filter;
- Vertical Transport: Crank-Nicholson;
- Dry deposition: resistance-based approach;
- Wet deposition: scavenging approach;
- Gas chemical mechanism: SAPRC97 (modified);
- Kinetic Gas solver: LSODE.

Test case 1: Off line DA

Test features

- Period: 2004/01/01-2004/12/31
- DA measurements: ground O3 max8h;
- DA output: O3 max8h;
- Assimilation interval: Day.

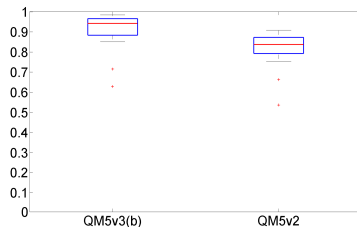


Test case 1: Off line DA

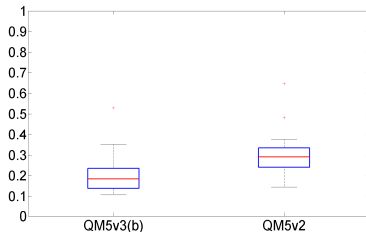
Test features

- Period: 2004/01/01-2004/12/31
- DA measurements: ground O3 max8h;
- DA output: O3 max8h;
- Assimilation interval: Day.

Correlation (Max8h)



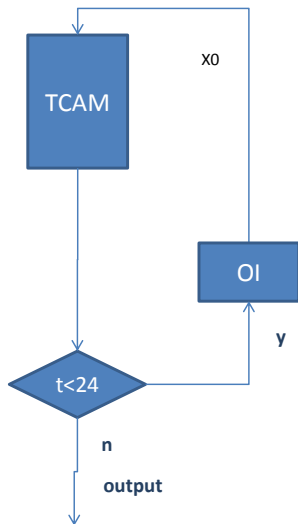
NMAE (Max8h)



Test case 2: On line DA

Test features

- Period: 2004/07/15-2004/07/31
- DA measurements: ground O3;
- DA output: O3 hourly mean;
- Assimilation interval: Hour;

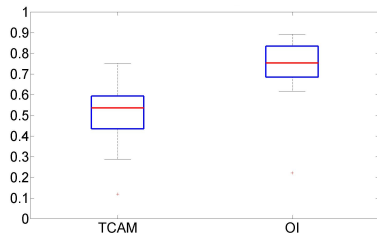


Test case 2: On line DA

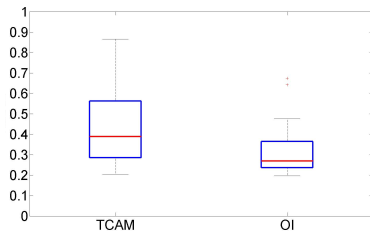
Test features

- Period: 2004/07/15-2004/07/31
- DA measurements: ground O3;
- DA output: O3 hourly mean;
- Assimilation interval: Hour;

Correlation



NMAE



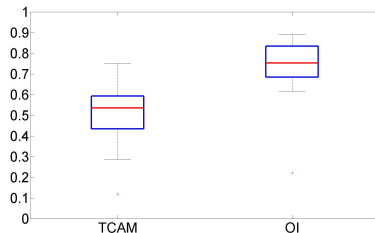
Test case 2: On line DA

Test features

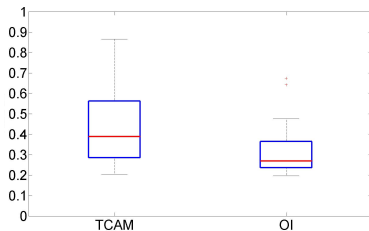
- Period: 2004/07/15-2004/07/31
- DA measurements: ground O3;
- DA output: O3 hourly mean;
- Assimilation interval: Hour;

unrealistic

Correlation



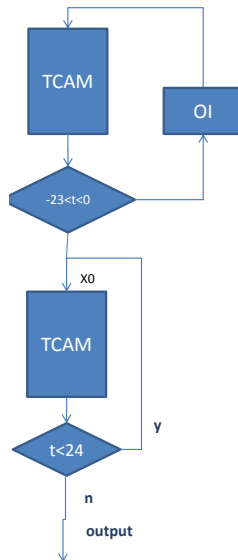
NMAE



Test case 3: Realistic On line DA

Test features

- Period: 2004/07/15-2004/07/31
- DA variable: O3 hourly mean;
- DA measurements: ground O3;
- DA output: O3 hourly mean;
- Assimilation interval: 24-hour day $d - 1$.

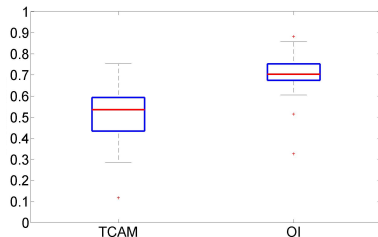


Test case 3: Realistic On line DA

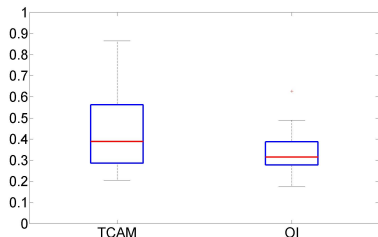
Test features

- Period: 2004/07/15-2004/07/31
- DA variable: O3 hourly mean;
- DA measurements: ground O3;
- DA output: O3 hourly mean;
- Assimilation interval: 24-hour day $d - 1$.

Correlation



NMAE



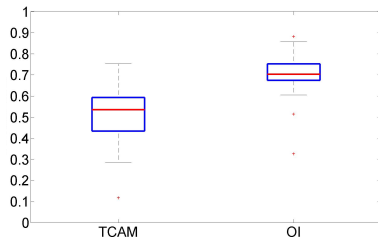
Test case 3: Realistic On line DA

Test features

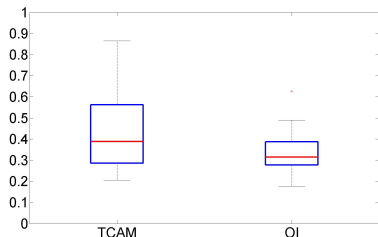
- Period: 2004/07/15-2004/07/31
- DA variable: O3 hourly mean;
- DA measurements: ground O3;
- DA output: O3 hourly mean;
- Assimilation interval: 24-hour day $d - 1$.

more realistic

Correlation



NMAE

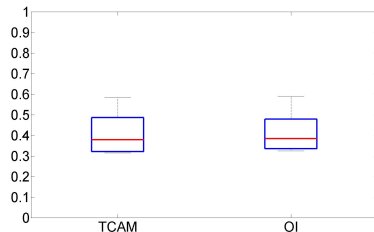


Test case 4: On line DA of Sat. Data

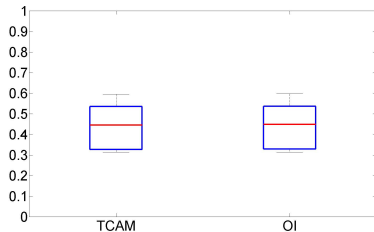
Test features

- Period: 2007/05/15-2005/07/31
- DA variable: NO2 hourly mean;
- DA measurements: OMI NO2;
- DA output: O3 hourly mean;
- Assimilation interval: ...;

Correlation



NMAE



Test case 4: On line DA of Sat. Data

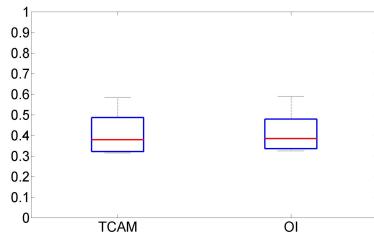
Test features

- Period: 2007/05/15-2005/07/31
- DA variable: NO2 hourly mean;
- DA measurements: OMI NO2;
- DA output: O3 hourly mean;
- Assimilation interval: ...;

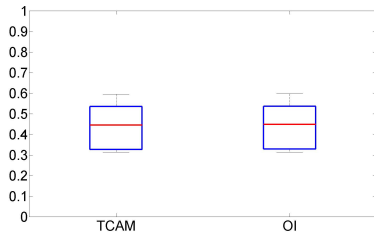
Too spot data!!!

... up to now...

Correlation



NMAE



Conclusions (?)

Off line DA

- Very high impact (expected);
- Increasing of performance even if the model performance are already good.

On line DA

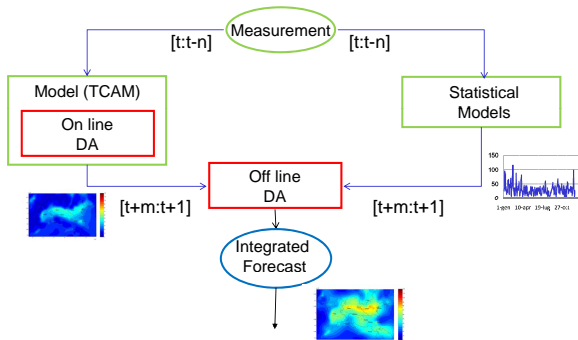
- ground measurements: relatively high impact;
- satellite measurements: difficult to evaluate (too few spot data!)... Larger dataset of measurements/model results needed.

Dream(?)

Merge Online & Offline DA techniques for better forecast
(Very) difficult, but...

Dream(?)

Merge Online & Offline DA techniques for better forecast
(Very) difficult, but...



TO BE CONTINUED...

Optimal Interpolation

$$x_a = x_b + K(y - Hx_b)$$

HP:

- $B = [b_{i,j}] = \exp(-\frac{d_{i,j}^2}{2L_h^2})v = D(i,j)v$
- $R = rI$

$$\begin{aligned} K &= D(i,j)vH^T(v(HD(i,j)H^T + \frac{r}{v}I))^{-1} \\ &= D(i,j)H^T(HD(i,j)H^T + \sigma I)^{-1} \end{aligned}$$

Optimal Interpolation

$$x_a = x_b + K(y - Hx_b)$$

HP:

- $B = [b_{i,j}] = \exp(-\frac{d_{i,j}^2}{2L_h^2})v = D(i,j)v$
- $R = rl$

$$\begin{aligned} K &= D(i,j)vH^T(v(HD(i,j)H^T + \frac{r}{v}I))^{-1} \\ &= D(i,j)H^T(HD(i,j)H^T + \sigma I)^{-1} \end{aligned}$$